

# Atomistic Molecular Simulations for Engineering Applications

Jadran Vrabec *et al.*



**Computational  
Molecular Engineering**

## Thermodynamic data from force fields gained recognition



ELSEVIER

journal h

### Fundamental equation of state based on experimental and molecular simulation data

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#### ARTICLE INFO

##### Article history:

Received 31 August 2015  
 Received in revised form 23 September 2015  
 Accepted 23 September 2015  
 Available online 23 October 2015

##### Keywords:

Thermodynamic properties  
 Fundamental equation of state  
 Molecular modeling and simulation  
 Hexamethyldisiloxane

#### A B S T R A C T

An empirical equation of state for hexamethyldisiloxane is presented. The equation is based on experimental data and molecular simulation results. The equation is valid for the temperature range 220 K to 570 K and for pressures up to 130 MPa. The equation is used to calculate thermodynamic properties of hexamethyldisiloxane at 130 MPa and 600 MPa.

REFPROP (MM) - NIST Reference Fluid Properties (DLL version 10.0)

File Edit Options Substance Calculate Plot Window Help Cautions

MM - C6H18OSi2 - Hexamethyldisiloxane (CAS# 107-46-0)

|                        |                    |                          |                          |
|------------------------|--------------------|--------------------------|--------------------------|
| Molar mass             | Triple point temp. | Normal boiling point     | Gas dipole at NBP        |
| 162,38 kg/kmol         | 204,93 K           | 373,66 K                 | 0,801 debye              |
| Critical Point         |                    |                          |                          |
| Temperature            | Pressure           | Density                  | Acentric factor          |
| 518,7 K                | 1,9311 MPa         | 268,41 kg/m <sup>3</sup> | 0,418                    |
| Range of applicability |                    |                          |                          |
| Min. temperature       | Max. temperature   | Maximum pressure         | Maximum density          |
| 204,93 K               | 580, K             | 130, MPa                 | 855,73 kg/m <sup>3</sup> |

NIST Rec: FEQ Helmholtz equation of state for hexamethyldisiloxane of Thol et al. (2016).

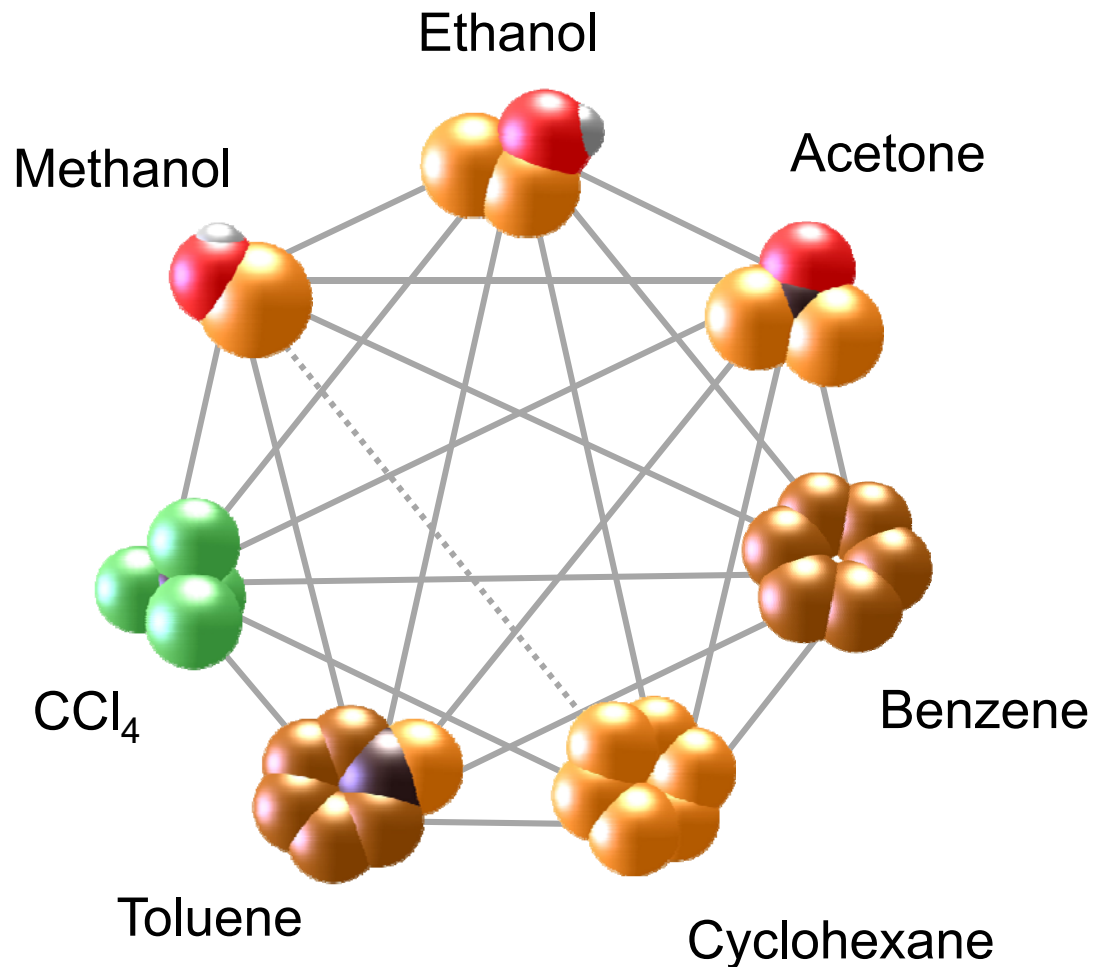
Thol, M., Dubberke, F.H., Rutkai, G., Windmann, T., Köster, A., Span, R., and Vrabec, J., "Fundamental Equation of State Correlation for Hexamethyldisiloxane Based on Experimental and Molecular Simulation Data," Fluid Phase Equilib., 418:133-151, 2016. doi: 10.1016/j.fluid.2015.09.047

The range of validity based on the experimental data is T = 220 K to 570 K with a maximum pressure of 130 MPa. The uncertainties in vapor pressure are 0.2% for T <= 410 K and 2% for higher temperatures. Homogeneous density data can be calculated with uncertainties of 0.2% in the liquid phase and 1% in the gas phase. The uncertainty for speed of sound data in the liquid phase is 0.5%. The uncertainty in the isobaric heat capacity is 0.2% in the gas phase and 1% in the liquid phase.

Link to publication: [DOI: 10.1016/j.fluid.2015.09.047](https://doi.org/10.1016/j.fluid.2015.09.047)

|                   |              |                      |
|-------------------|--------------|----------------------|
| Equation of State | Viscosity    | Thermal Conductivity |
| Surface tension   | Melting Line | Sublimation Line     |
| OK                | Cancel       | Copy                 |
|                   |              | Copy All             |
|                   |              | Print                |

## Transport properties



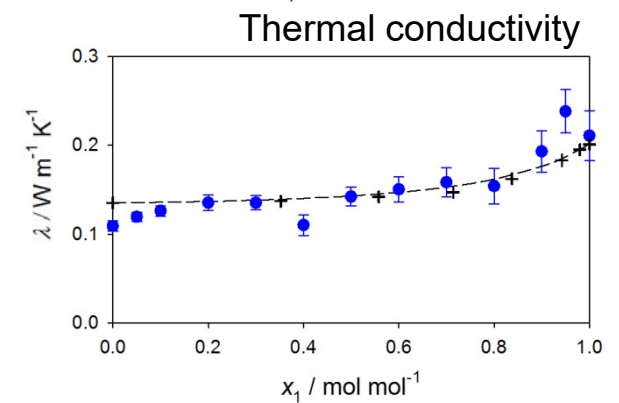
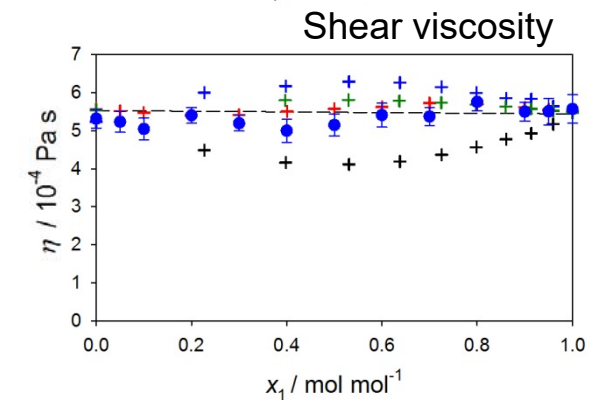
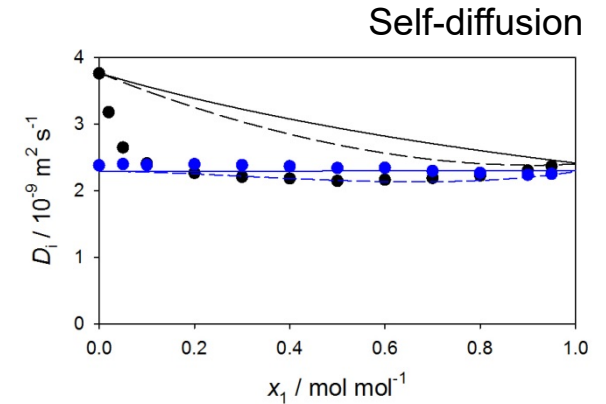
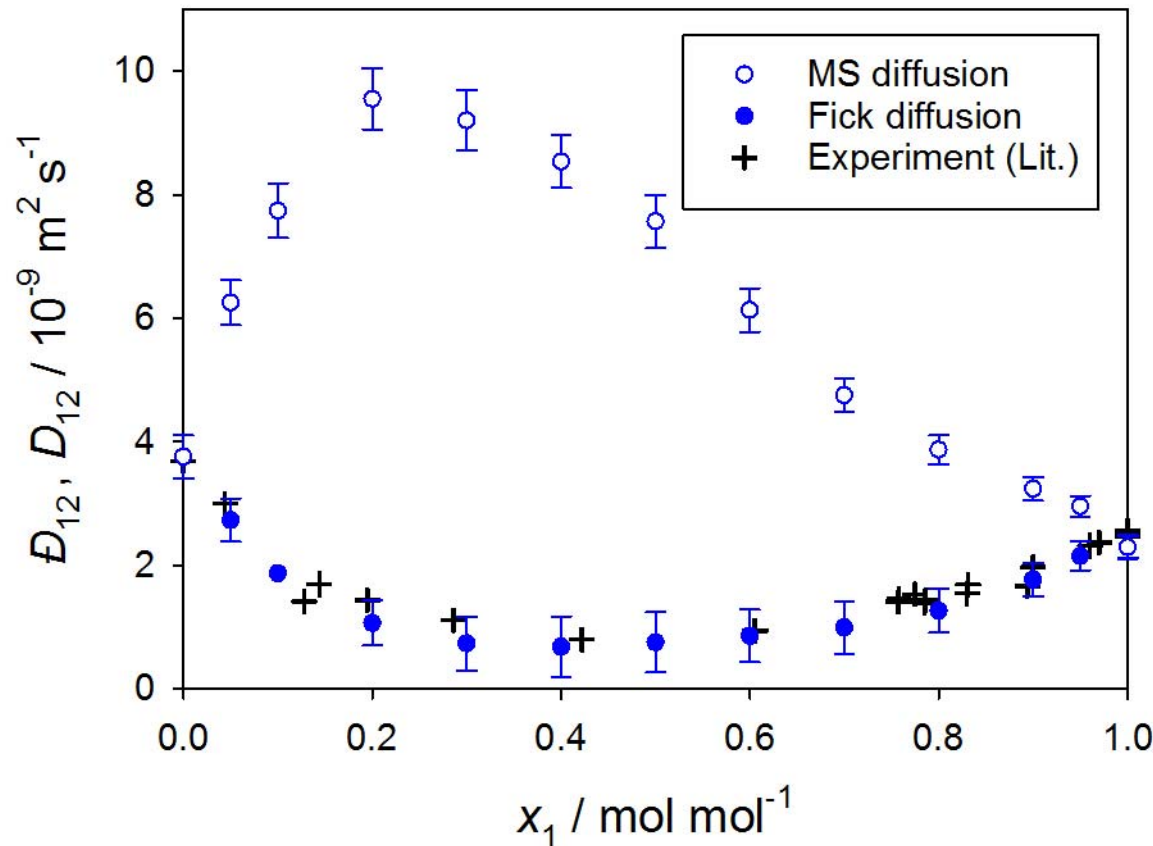
- Molecular models
- Rigid molecules (united atom)
- Lennard-Jones sites, point charges, dipoles, quadrupoles
- Parameters optimized to saturated liquid density and vapor pressure (partly also self-diffusion)
- Mixing behavior: predicted

**20 binary mixtures**

Guevara-Carrion et al.,  
*J. Chem. Phys.* **144**, 124501 (2016)

## Example: Methanol + Toluene

### Diffusion coefficients



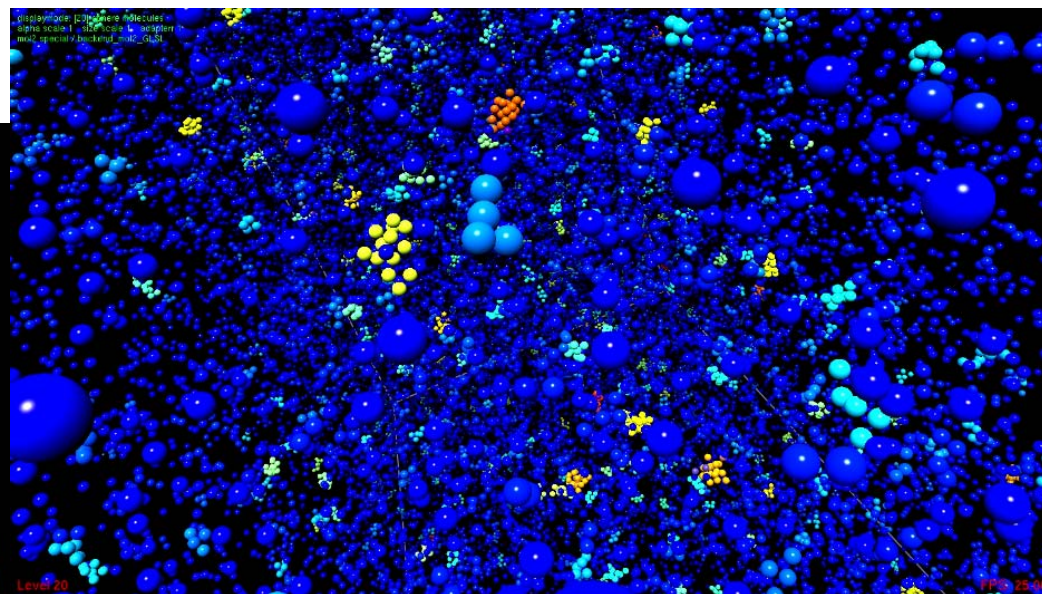
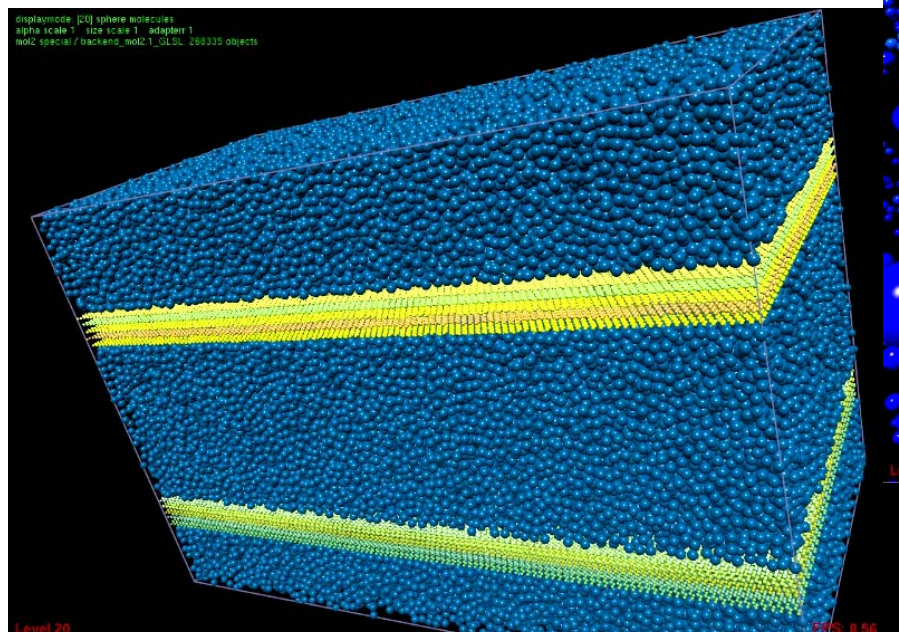


## Massively parallel molecular dynamics code: *ls1*

- Force fields: Rigid, Lennard-Jones based, incl. electrostatics
- Tersoff potential for solids
- „Large“ systems, „long“ time scales
- Concurrency in space, not in time

Nucleation

Flow

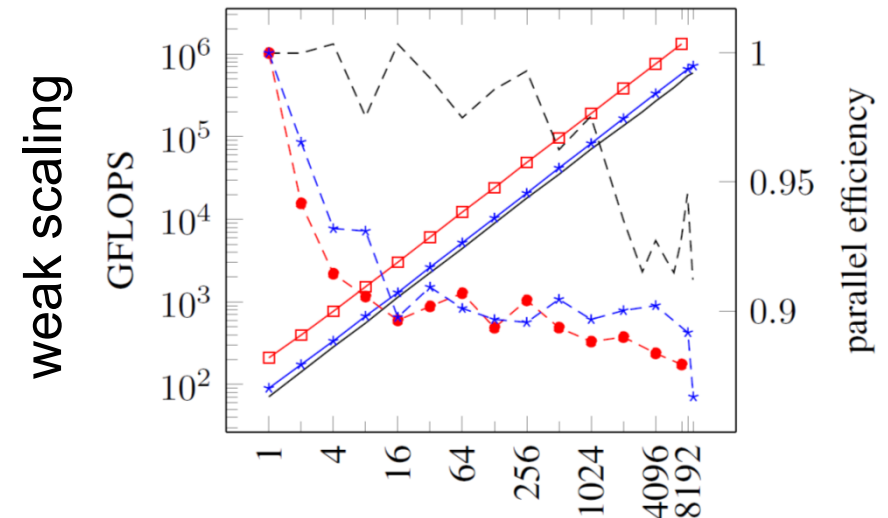


Niethammer et al.,  
*J. Chem. Theory Comput.* **10** (2014) 4455

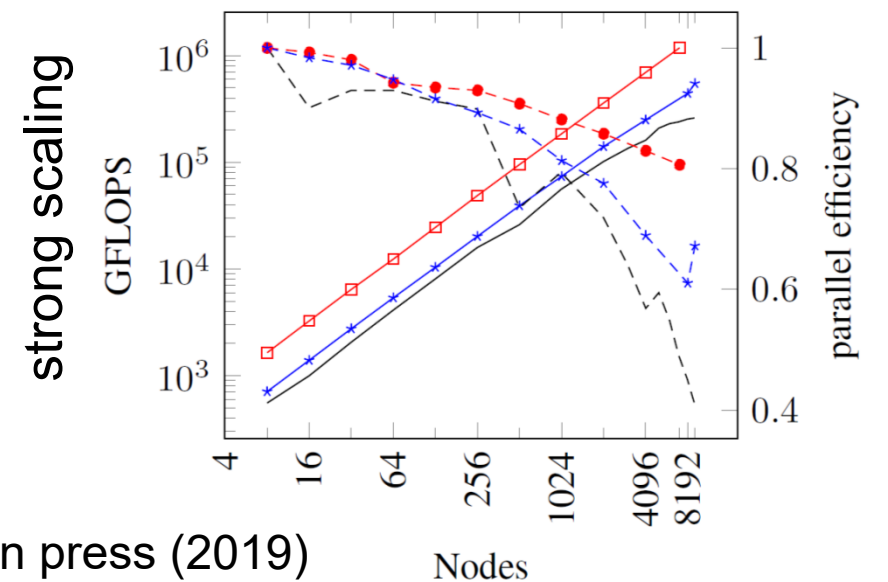
## 21 trillion molecules simulation on Hazel Hen



- **max.  $2.1 \cdot 10^{13}$  molecules**
- 1.33 PFLOPS absolute performance
- 88% weak scaling efficiency
- 80% strong scaling efficiency
- 9% of single precision peak performance

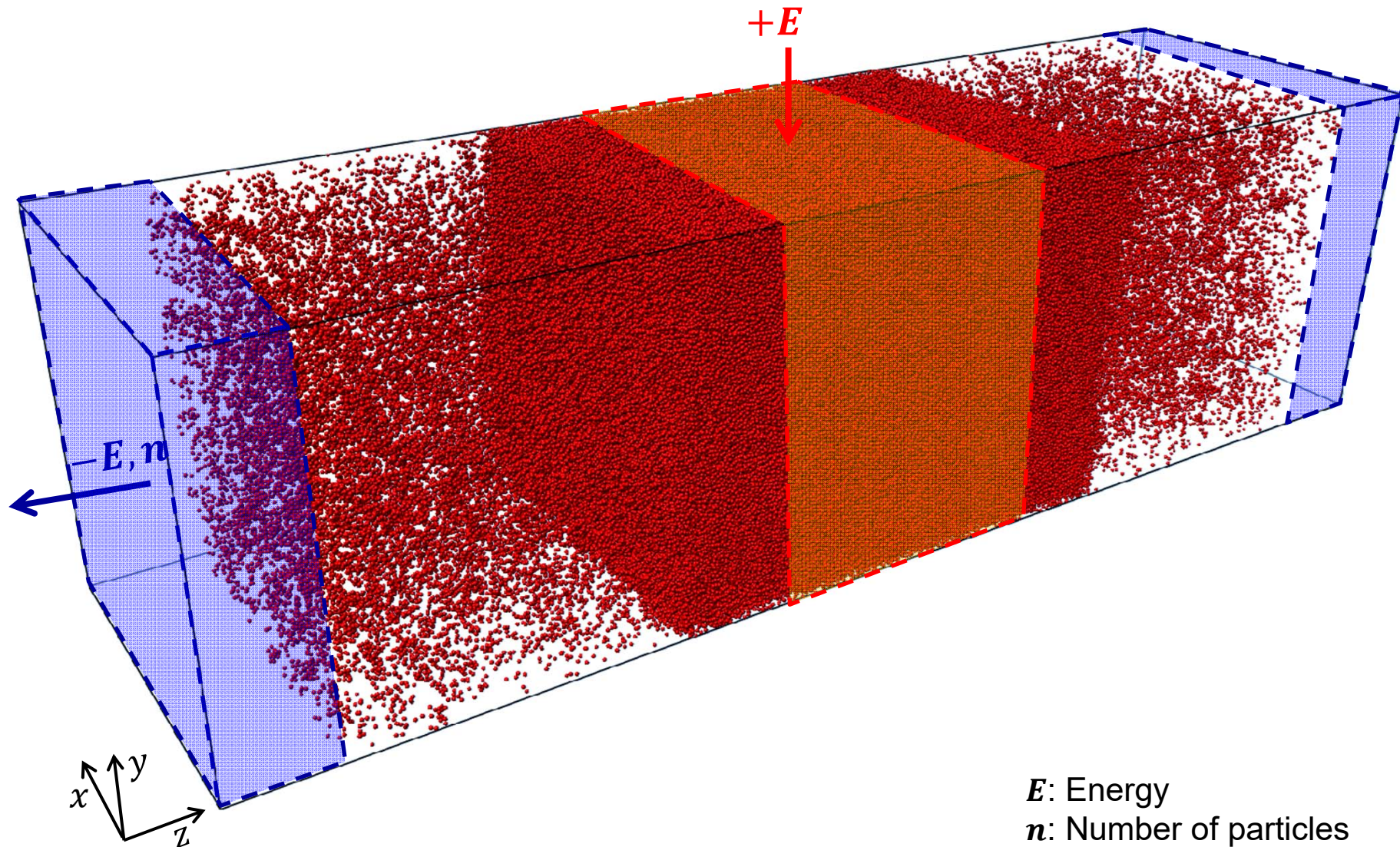


— Hazel Hen — SuperMUC





## Simulation of evaporation with /s1

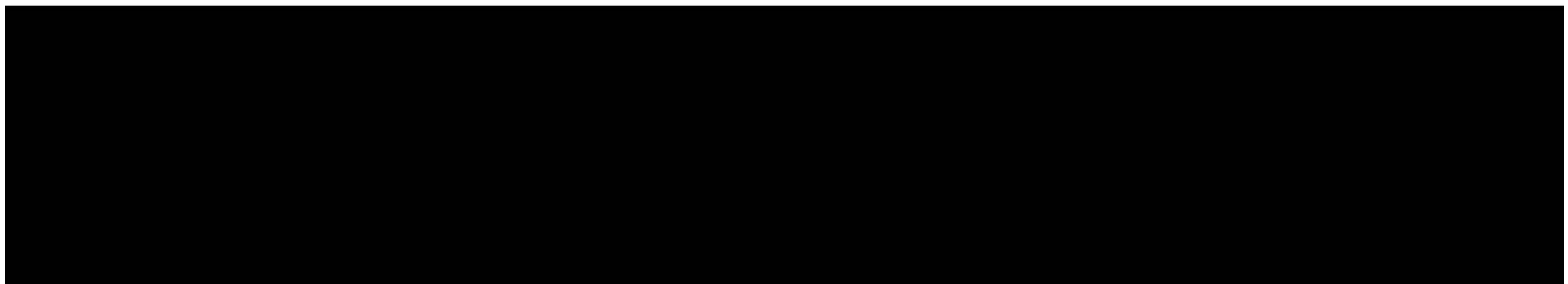
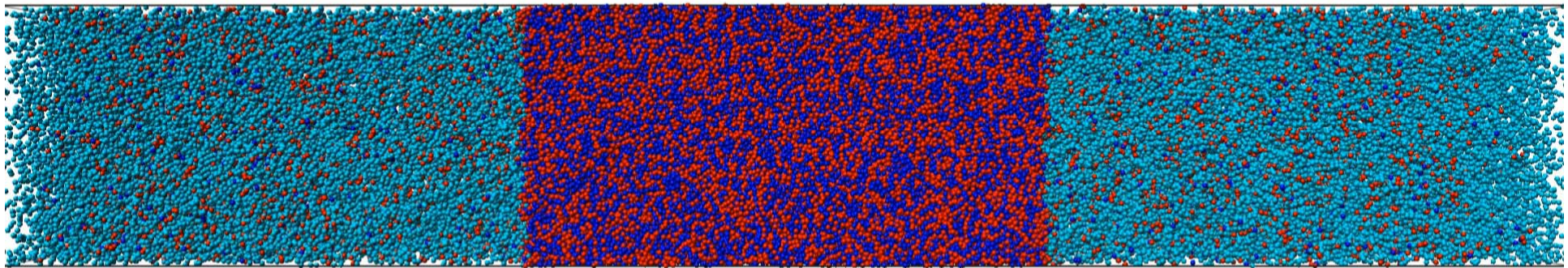
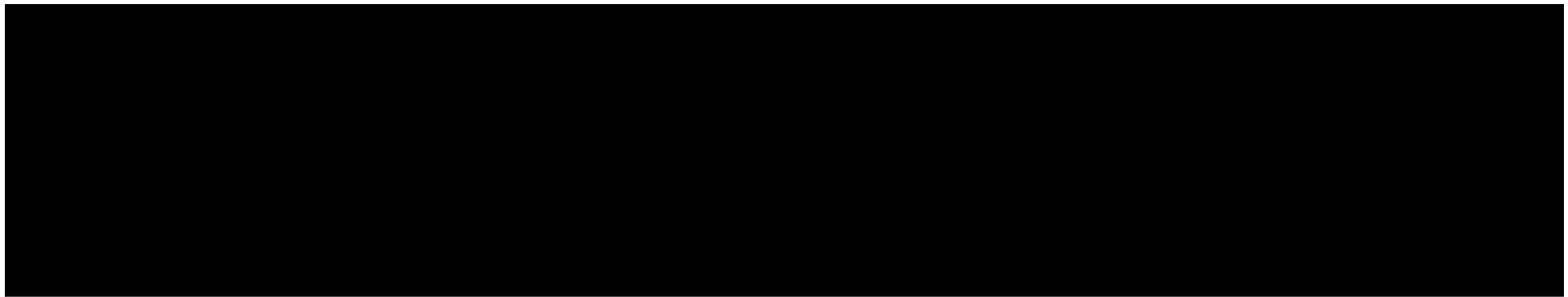


$E$ : Energy  
 $n$ : Number of particles



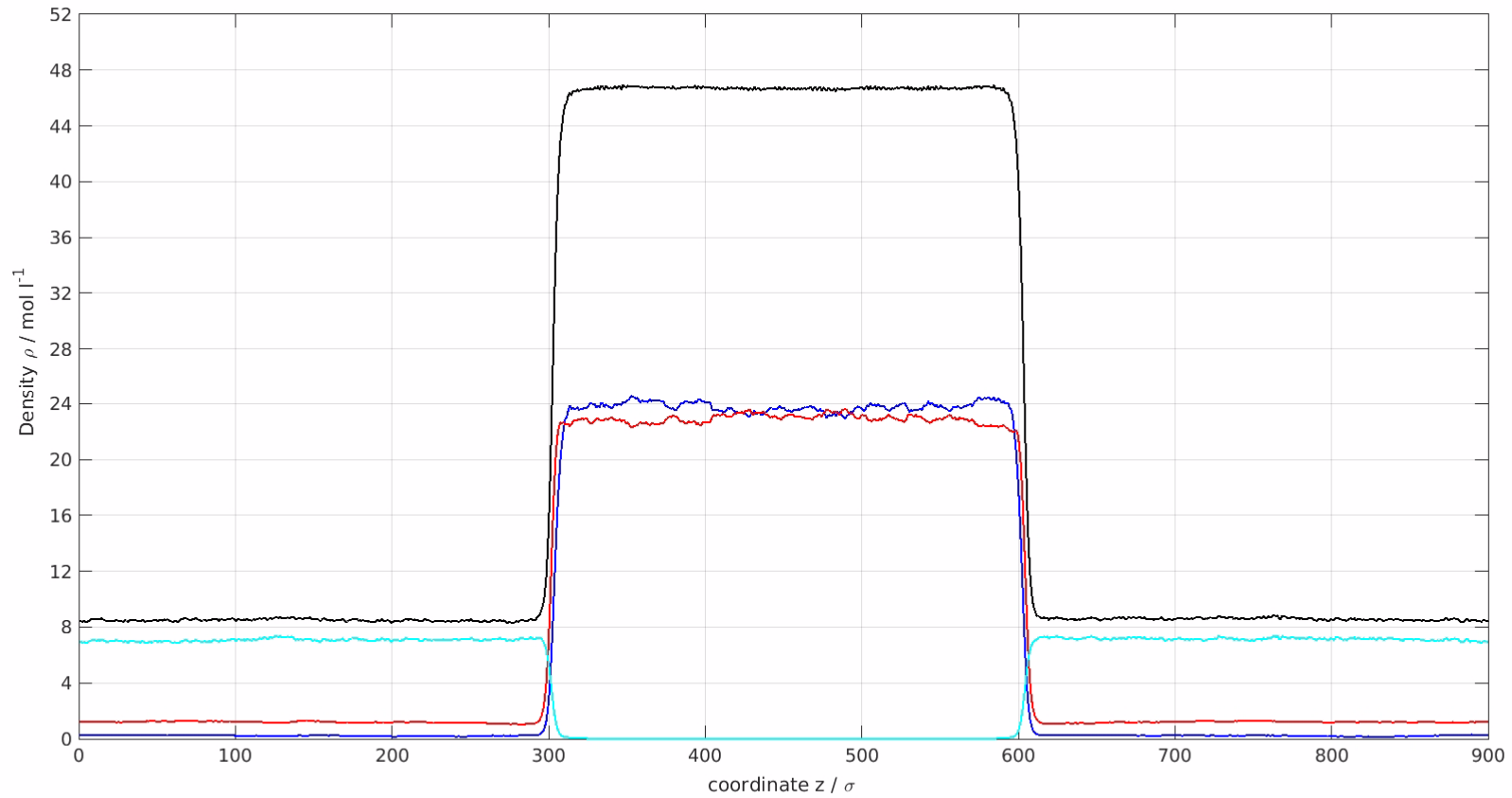
## Simulation of evaporation with /s1

Equimolar LJ mixture evaporating through a very dense gas (~isothermal)



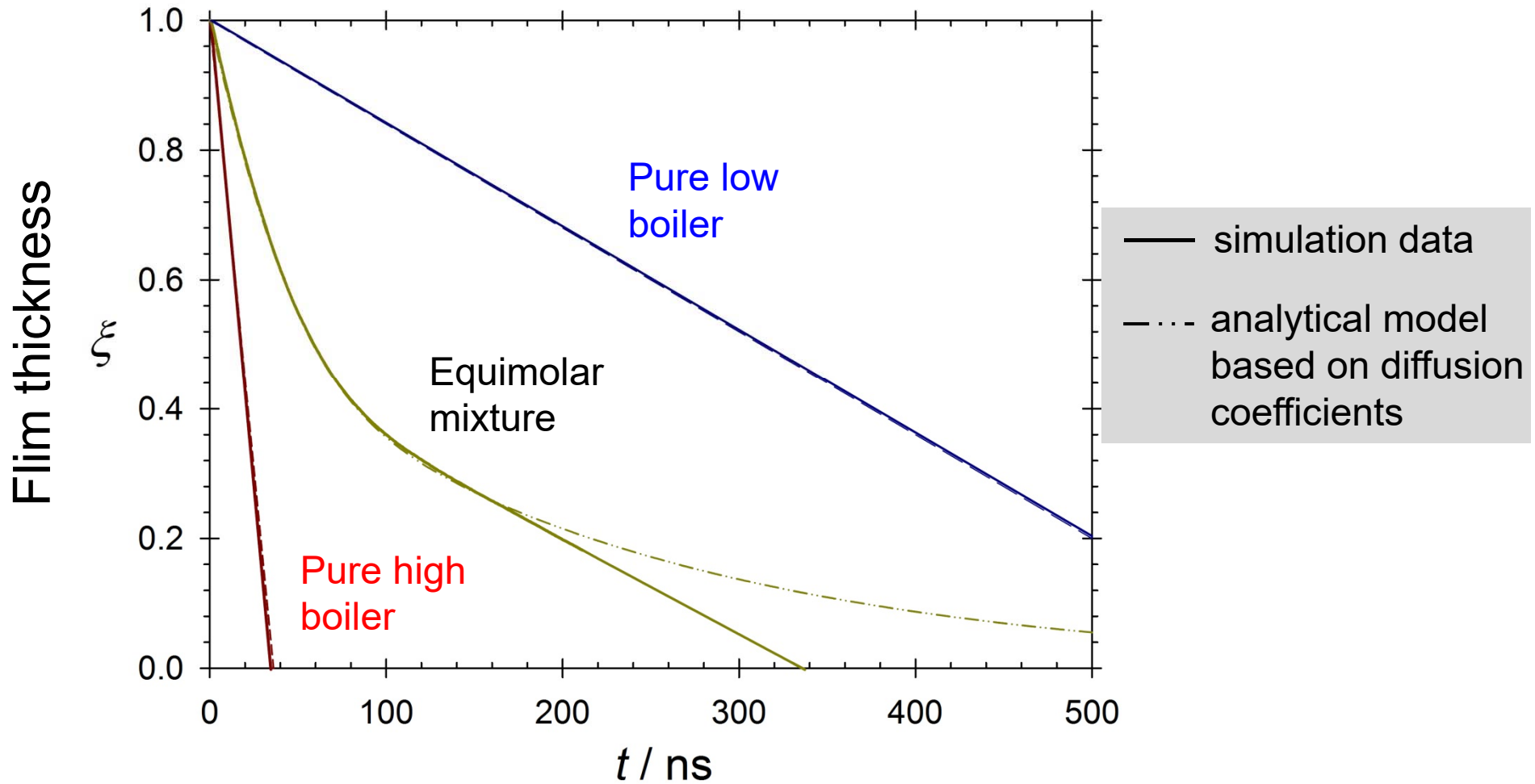
# Time dependence of partial densities during evaporation

... spatially resolved



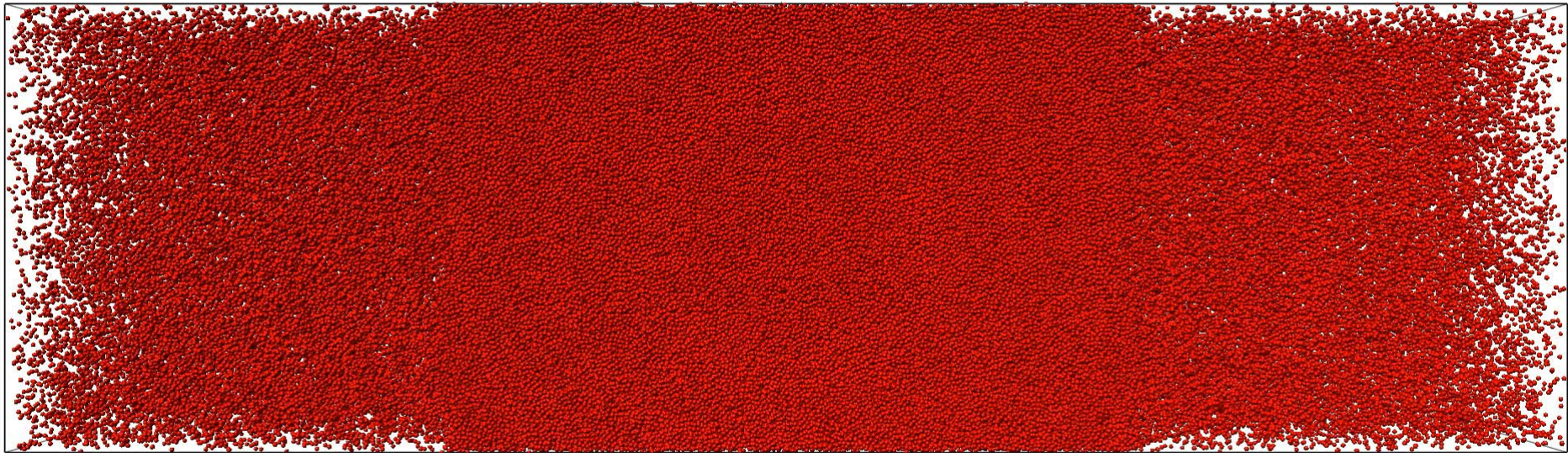
Coordinate /  $\sigma$

## “D-squared law” for planar film

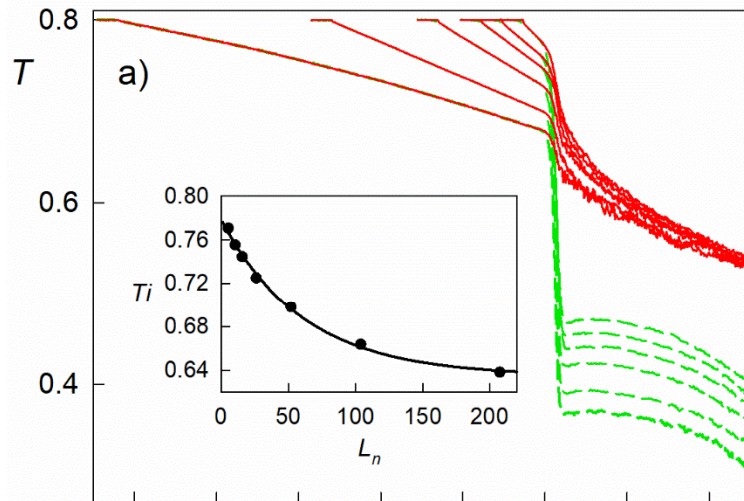




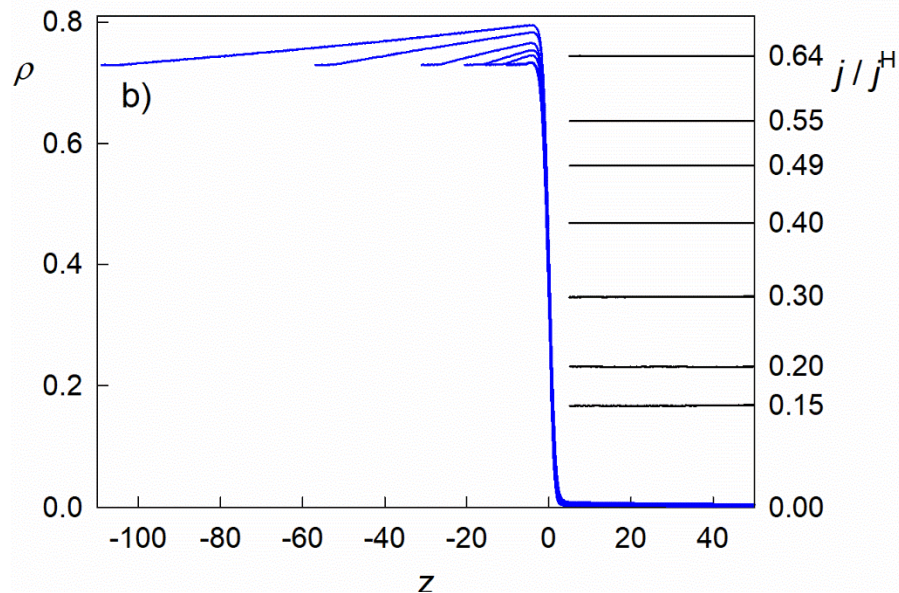
## Quasi-stationary simulation of evaporation



## Distance between thermostat region and interface $L_n$



- $L_n$  Distance to thermostat
- $T_{xy}$  Temperature in x, y directions
- - -  $T_z$  Temperature in z direction
- $T_i$  Interface temperature
- $\rho$  Density
- $j/j^H$  Molar flux / Hertz flux



Molar flux  $j$  only depends  
 on interface temperature  $T_i$

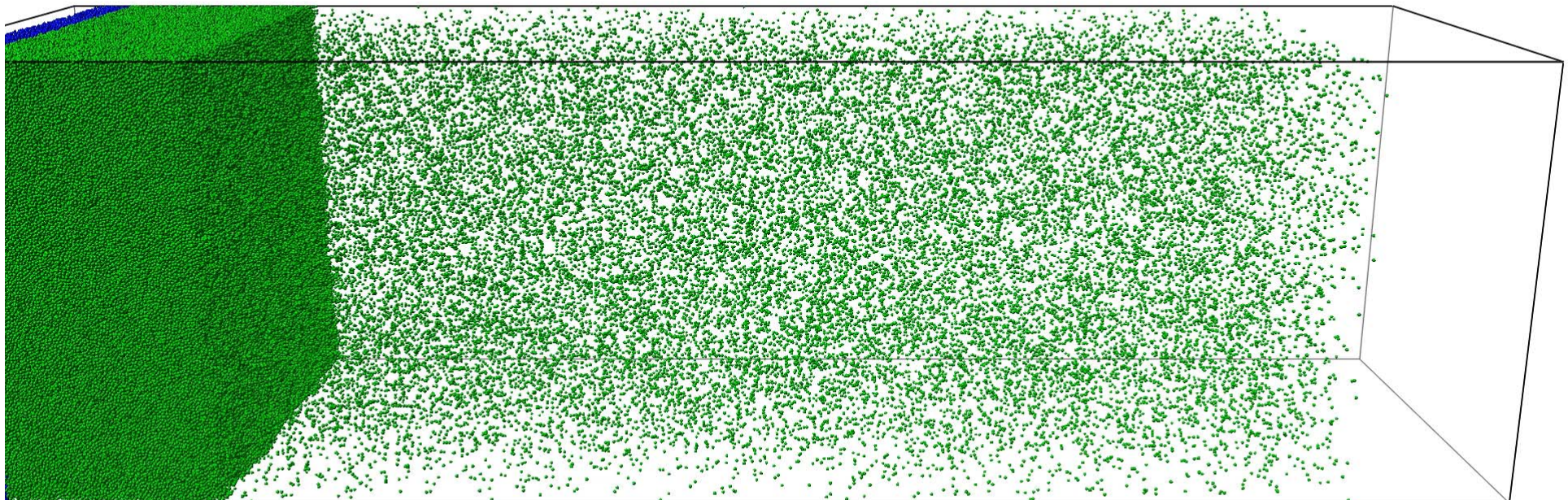
| $L_n$ | $T_l$  | $T_i$  | $j \cdot 10^3$ |
|-------|--------|--------|----------------|
| 5.2   | 0.8000 | 0.7705 | 4.504          |
| 10.4  | 0.8240 | 0.7740 | 4.523          |
| 15.6  | 0.8466 | 0.7712 | 4.496          |

Heinen et al.,  
*J. Chem. Phys.* **145**: 081101 (2016)



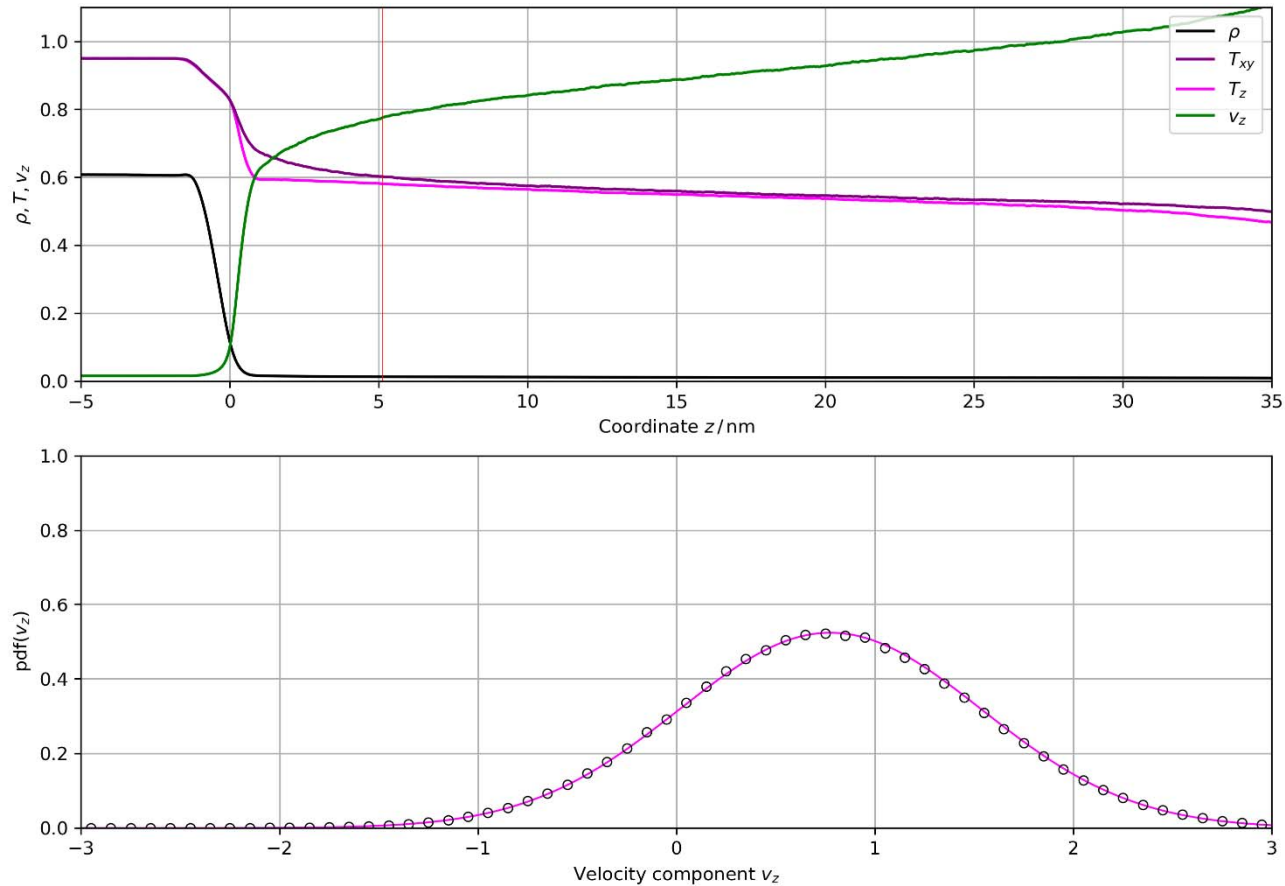
## Stationary simulation of evaporation

Fresh liquid is supplied from the left side to attain constant interface position



## Temperature, density and velocity profiles @ $T_i^*=0.95$

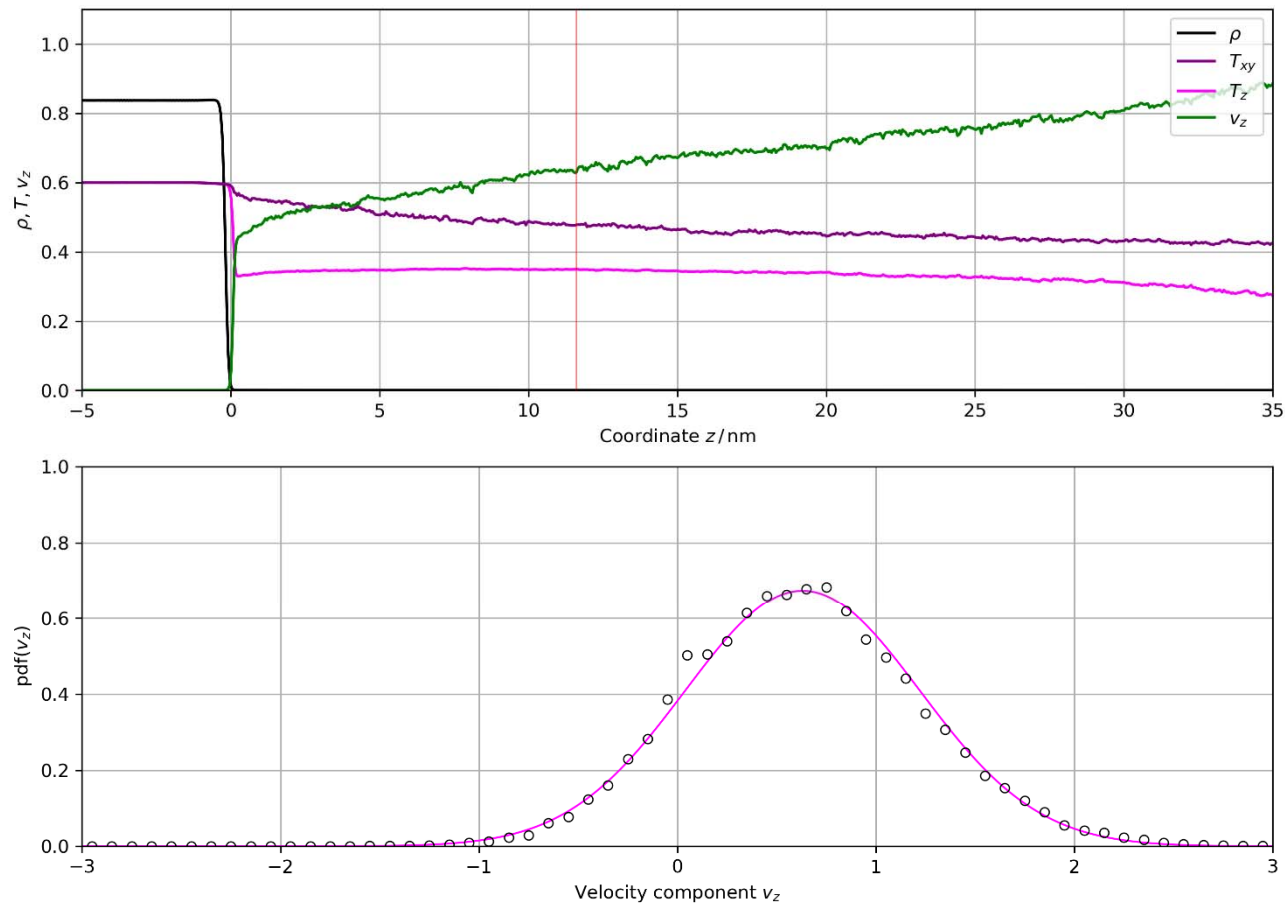
Velocity distribution function is Maxwellian everywhere



## Temperature, density and velocity profiles @ $T_i^*=0.6$

Velocity distribution function is not Maxwellian at the interface

A thermalization region can be define in which the Maxwellian is re-attained



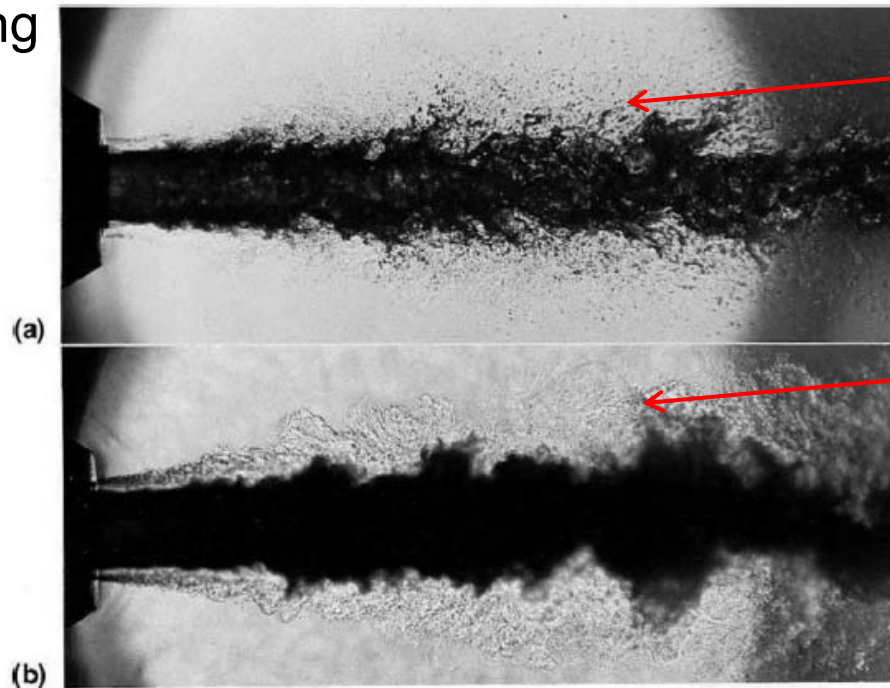


## Liquid nitrogen injection (instead of oxygen)

Dahms, Oefelein: Phys. Fluids 25 (2013)

Injector operating pressure:

$$p = 1 \text{ MPa}$$



Spray

Diffuse mixing

$$p = 6 \text{ MPa}$$

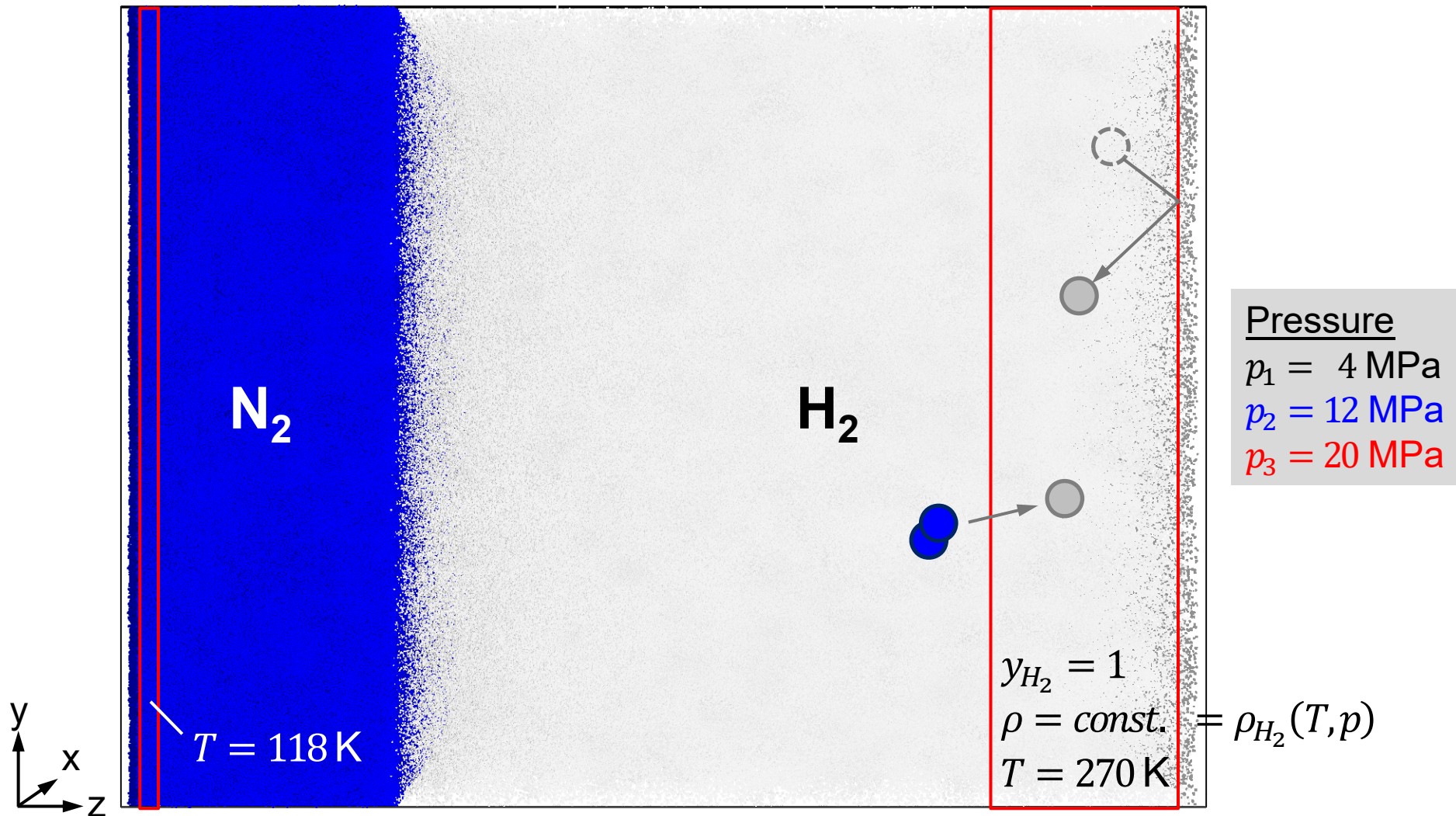
FIG. 1. Nonreacting shear-coaxial liquid-nitrogen–helium injector operating at (a) 1.0 MPa and (b) 6.0 MPa.  $T_{N_2} = 97 \text{ K}$ ,  $T_{He} = 280 \text{ K}$  into GHe at  $T = 300 \text{ K}$ . Reprinted with permission from W. Mayer, A. Schik, B. Vieille, C. Chaveau, I. Gökalp, D. Talley, and R. Woodward, *J. Propul. Power* **14**, 835 (1998). Copyright 1998, American Institute of Aeronautics and Astronautics.

Also, helium instead of hydrogen ...

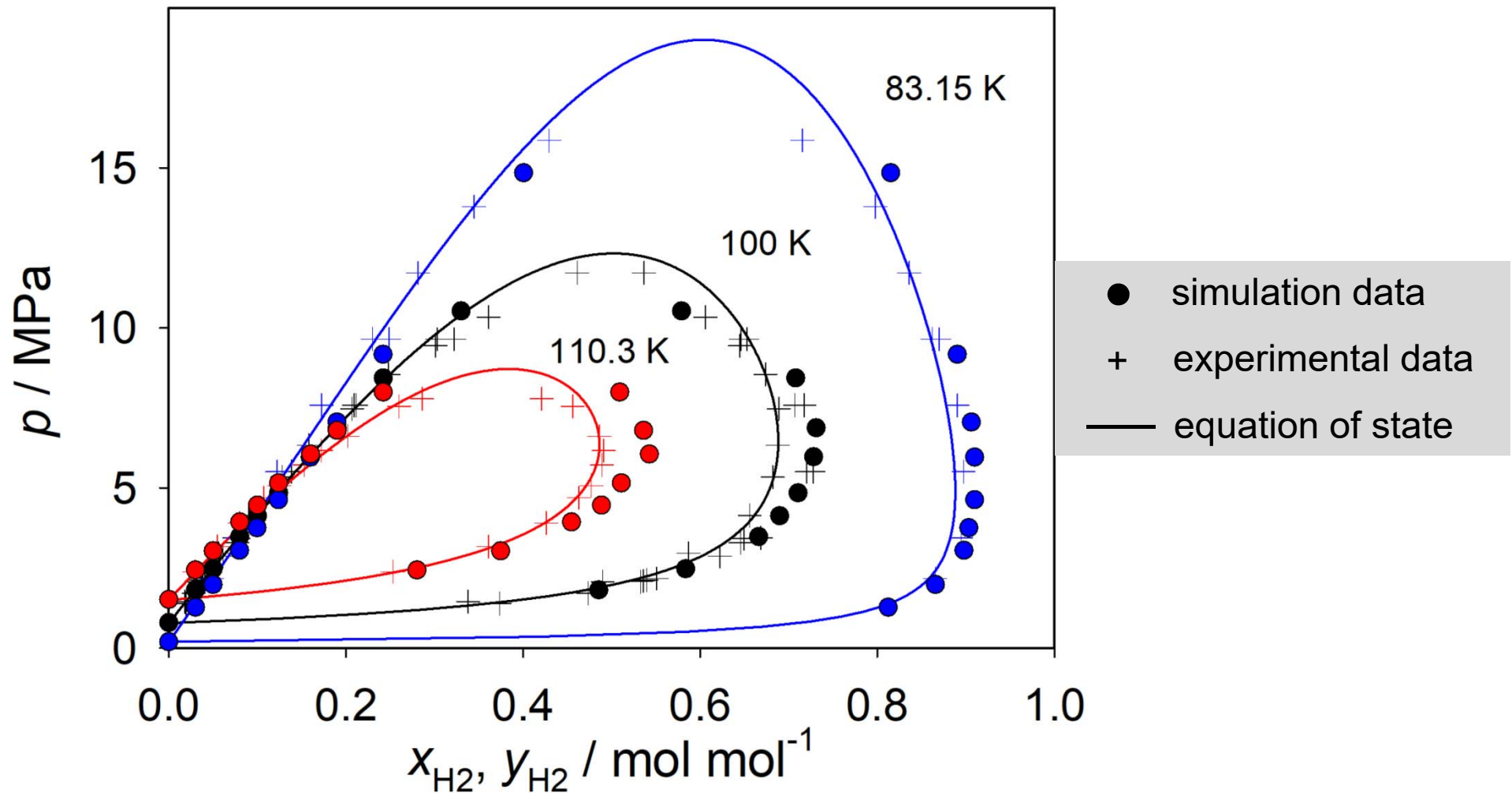


## Dual Control Volume (DCV)

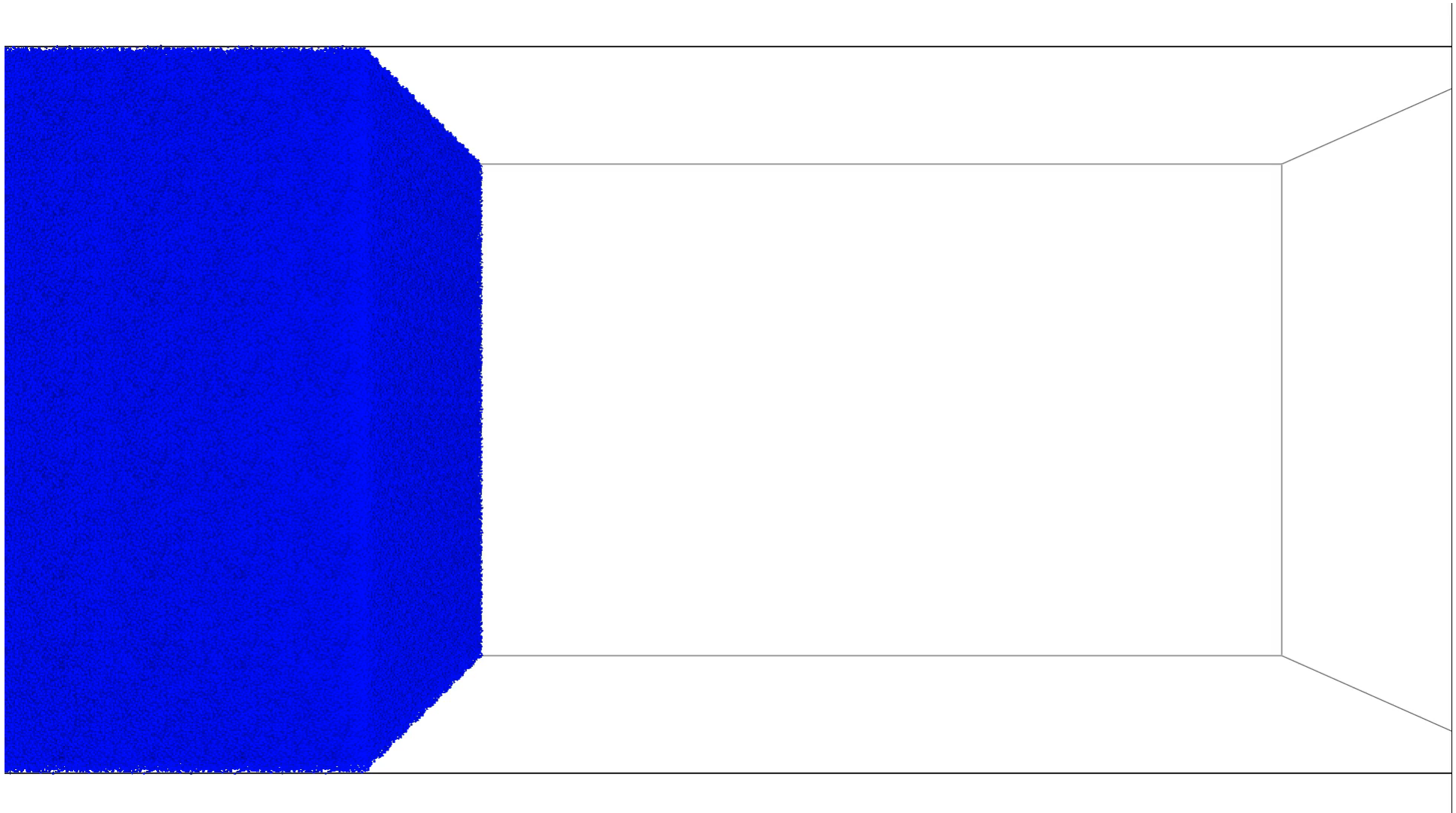
$$N \approx 10^7$$



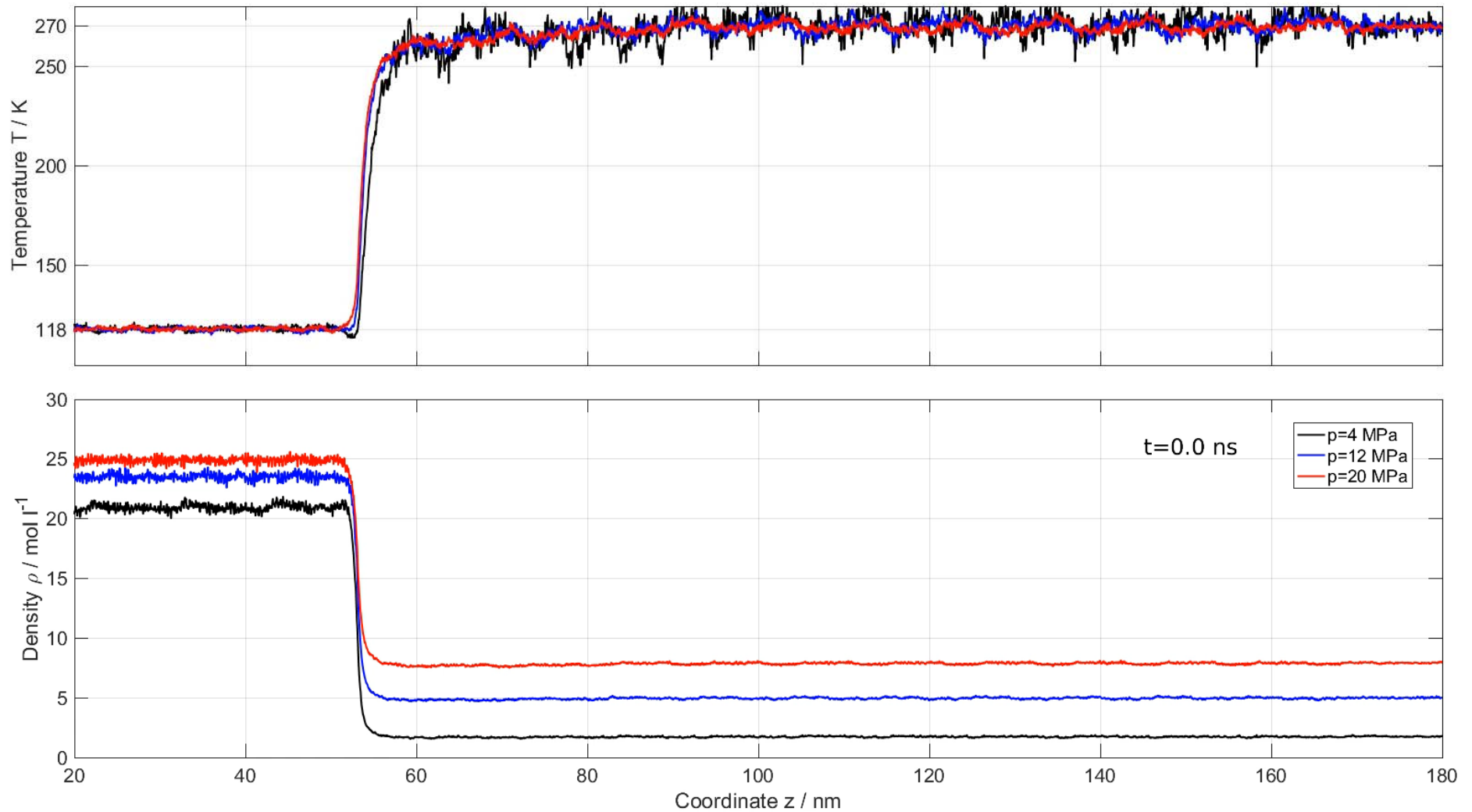
## Vapor-liquid phase diagram of $N_2 + H_2$



## Visualization: Liquid $N_2$ evaporating into $H_2$

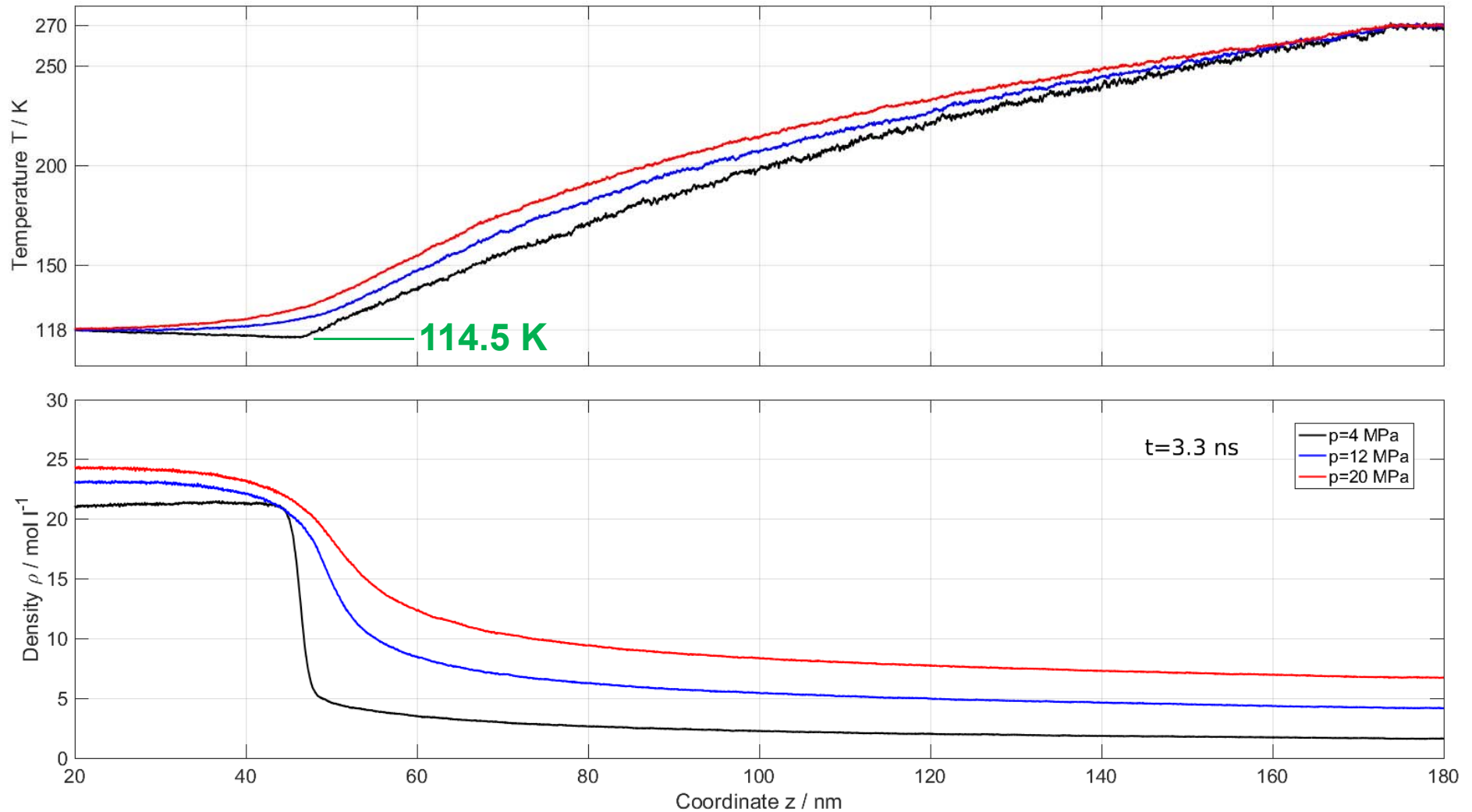


## Evolution of temperature and density





## Evolution of temperature and density



## Instationary simulation of a shock tube

A pure fluid at different densities interacts with itself

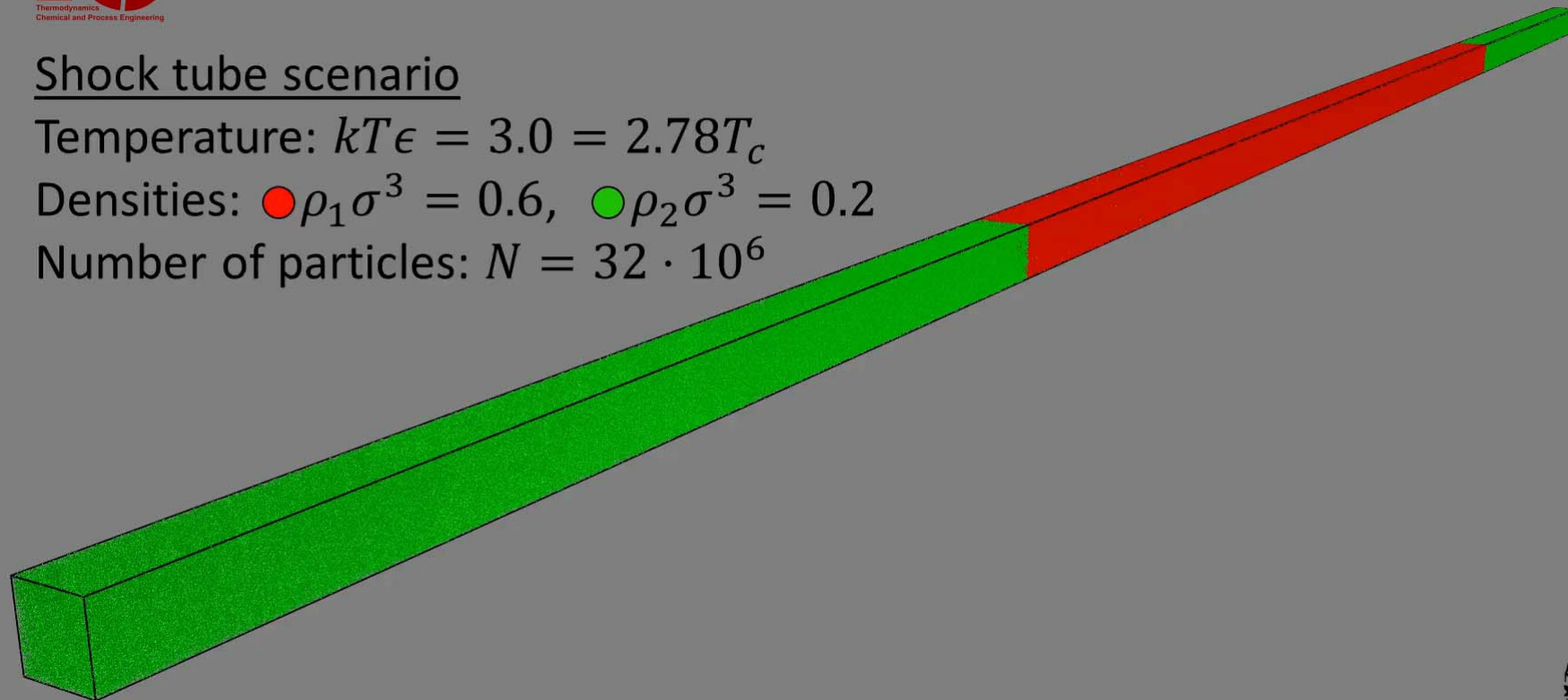


### Shock tube scenario

Temperature:  $kT\epsilon = 3.0 = 2.78T_c$

Densities: ●  $\rho_1\sigma^3 = 0.6$ , ●  $\rho_2\sigma^3 = 0.2$

Number of particles:  $N = 32 \cdot 10^6$

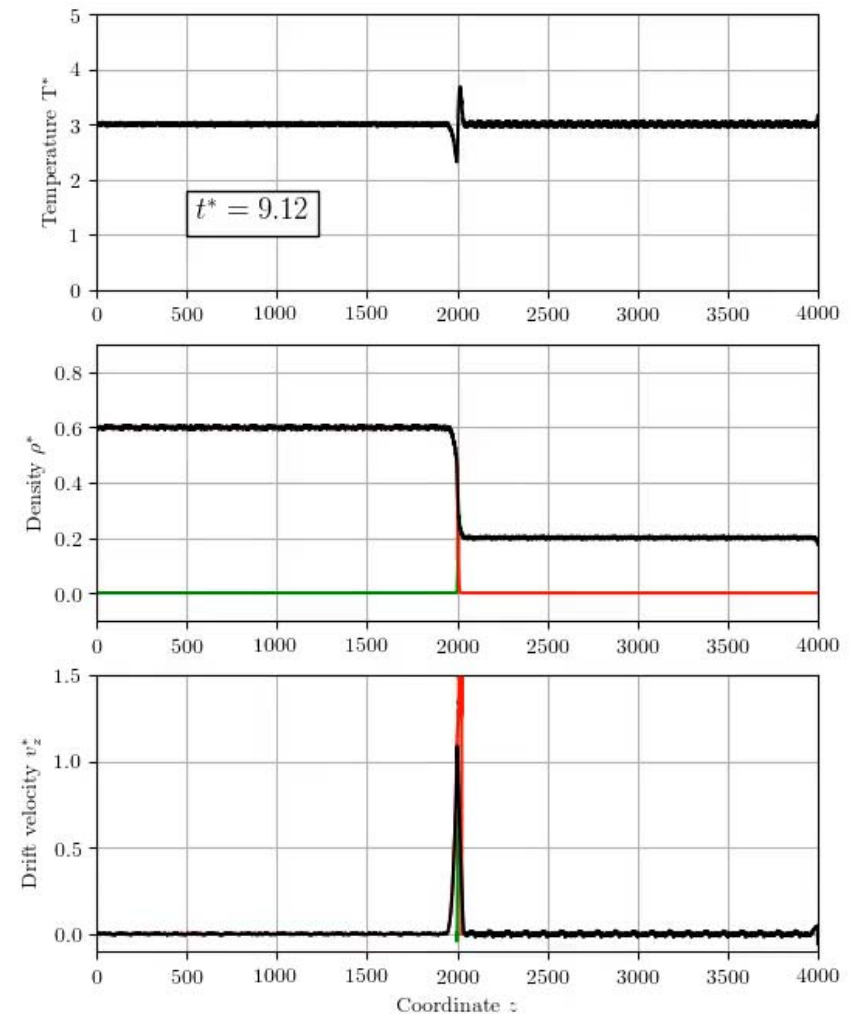




## Shock wave results

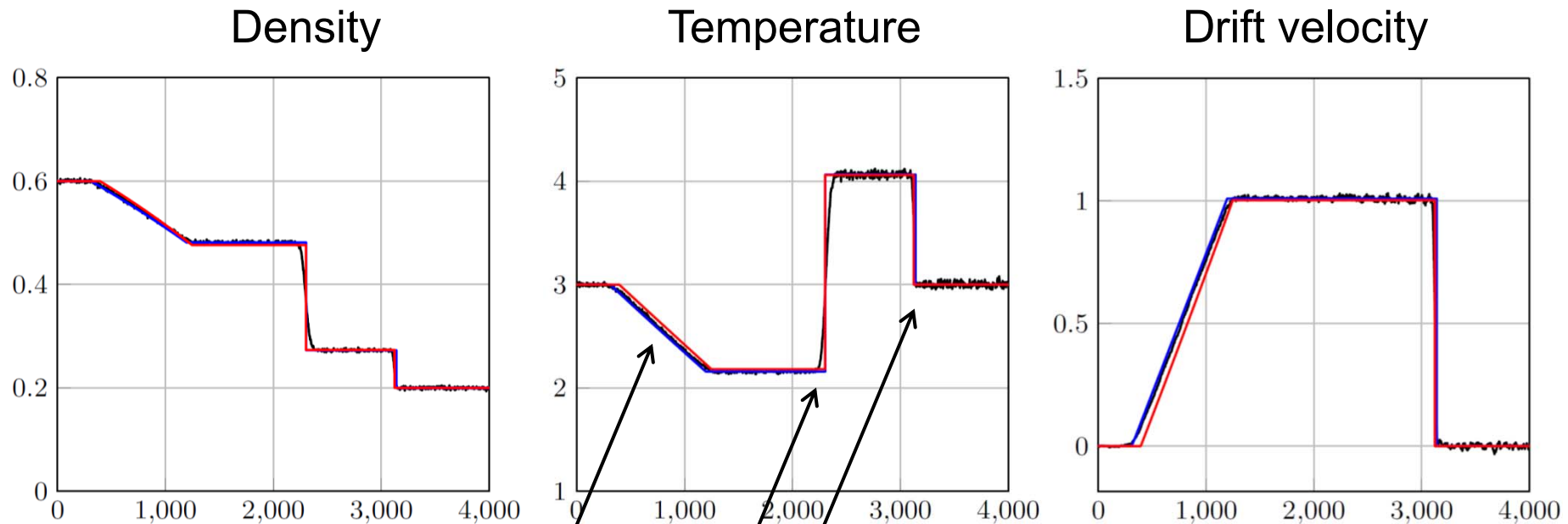
Circular marks are visible where the expanding spherical atmospheric shockwaves from the gun firing meet the water surface

- expanding phase
- stationary phase
- overall



## Results for shock wave ...

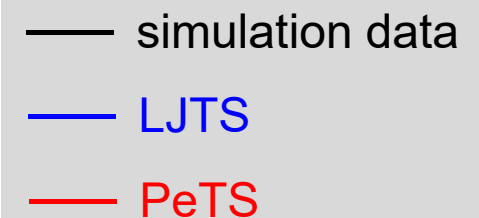
agree very well with discontinuous Galerkin spectral element solution of the multiphase Riemann problem (Hitz, Munz, IAG, University of Stuttgart)



Rarefaction wave

Contact discontinuity  
(material boundary)

Shock front



## Summary

- Classical force fields contain thermodynamic properties adequately
- Molecular dynamics simulations of inhomogeneous fluids may efficiently use large machines
- The spectrum of possible applications of molecular modeling and simulation is very wide



